Statistical Topic Models for Multi-Label Document Classification

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Automatic text categorization for multi-label documents

- Broad goal is classification of multi-label documents
- Multi-label data:
 - Each document can be assigned one or more labels
 - E.g., HEALTH and GENETICS and CANCER RESEARCH

Automatic text categorization for multi-label documents

- Broad goal is classification of multi-label documents
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 - Each document can be assigned one or more labels
 - E.g., HEALTH and GENETICS and CANCER RESEARCH
- Popular approach is binary SVMs

Classification of rare labels

"The skewed distribution of the Yahoo! Directory and other large taxonomies with many extremely rare categories makes the classification performance of SVMs unacceptable. More substantial investigation is thus needed to improve SVMs and other statistical methods for very large-scale applications."

-Liu et al. (2005), Support Vector Machines with a very large taxonomy

Accounting for label dependencies

"The consensus view in the literature is that it is crucial to take into account label correlations during the classification process However as the size of the multi-label data sets grows, most methods struggle with the exponential growth in the number of possible correlations. Consequently these methods are able to be more accurate on small data sets, but are not as applicable to larger data sets."

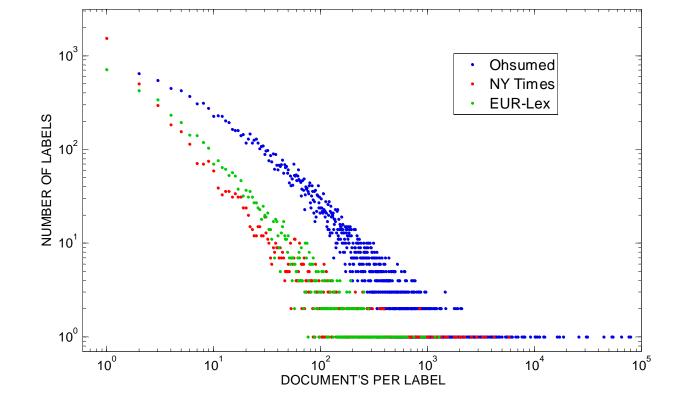
-Read et al. (2009), Classifier chains for multi-label classification

- 1. Classification of rare labels
- 2. Accounting for label dependencies

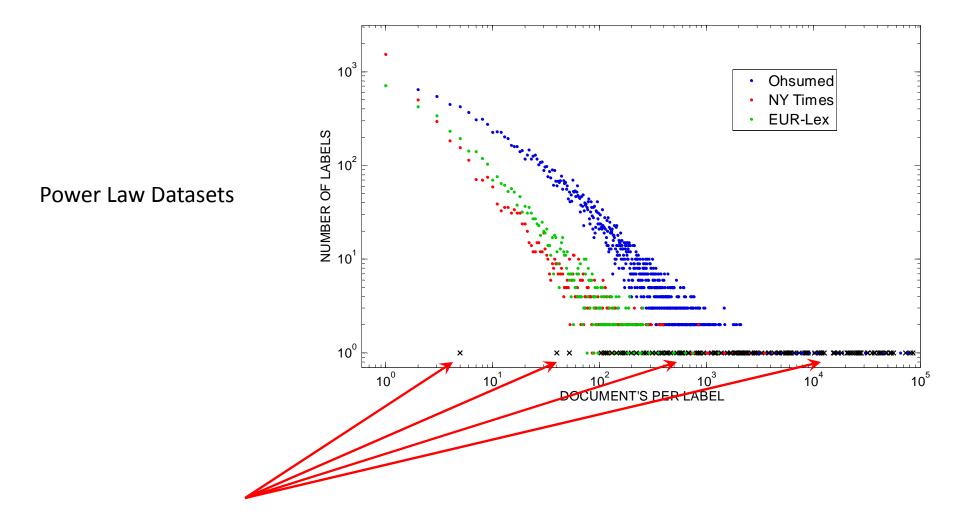
Have significant implications for real-world data

Mismatch between Real World data and Research Datasets

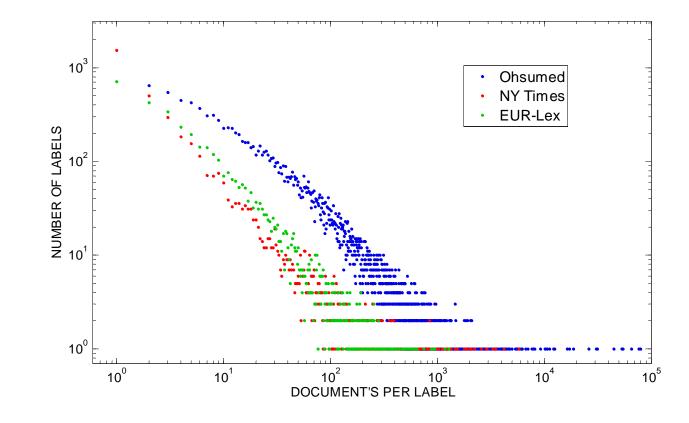
1. Many real world datasets have skewed labelfrequency distributions, with many rare labels



Power Law Datasets

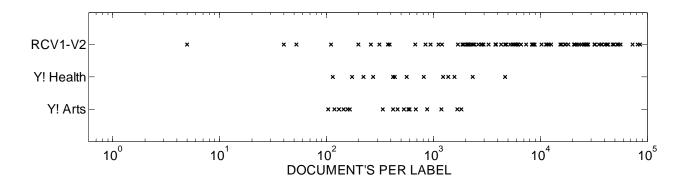


Benchmark Datasets



Power Law Datasets

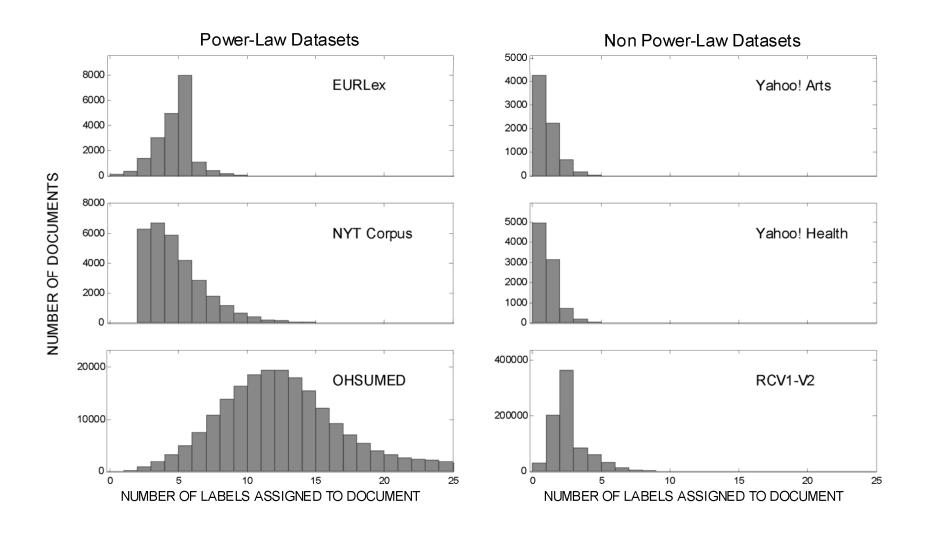




Mismatch between Real World data and Research Datasets

- 1. Real world datasets have skewed label-frequency distributions, with many rare labels
- 2. Real world data has many more labels per document than most benchmark data sets

Labels-Per-Document



Looking ahead...

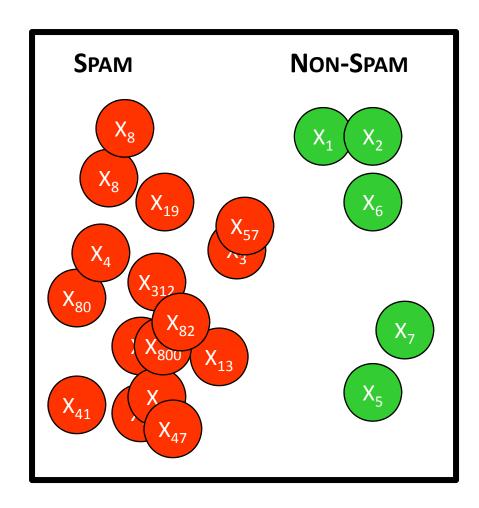
- Present a new probabilistic model that accounts for label dependencies
- Key results:
 - Large improvement over simpler probabilistic models
 - Good performance on rare labels
 - Model is highly competitive with discriminative methods on *real-world* data sets

Overview

- Research problem
 - Research goals and challenges
- Motivate probabilistic methods
 - Discussion of SVMs for multi-label data
- Present our probabilistic models
- Experimental Results

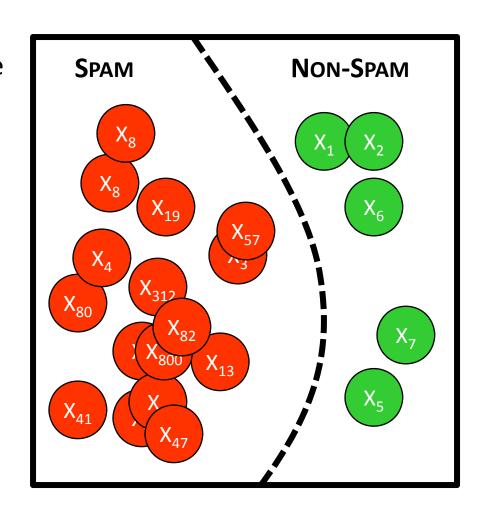
SVMs: Binary data

 SVMs (and many other classifiers) are designed for binary data



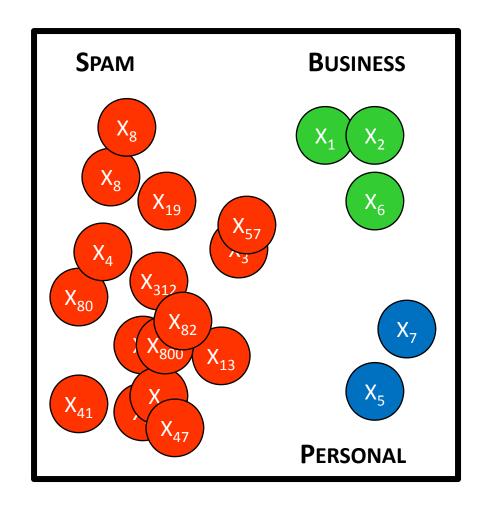
SVMs: Binary data

- SVMs (and many other classifiers) are designed for binary data
- Goal: Find a separating hyperplane



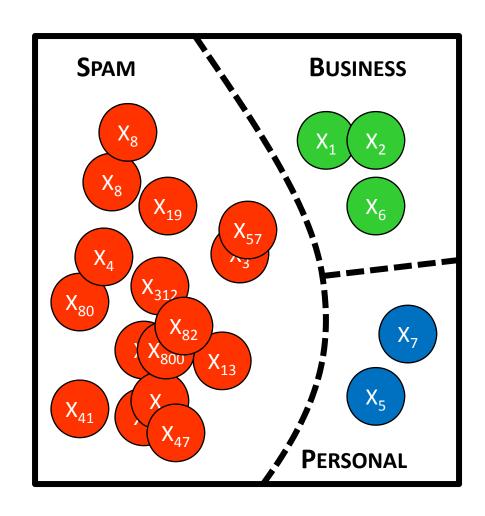
SVMs: Multiple Classes

- Often, we have more than two classes that we wish to predict
- For now, assume single label per document



SVMs: Multiple Classes

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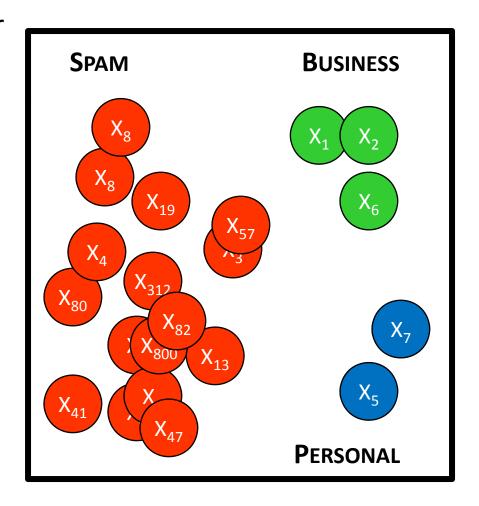
Binary Problem Transformation

- Popular approach:
 - Transform the problem into multiple binary classification problems
- "One-Vs-All" transformation
 - Note: applicable to any binary classifier

Binary Problem Transformation

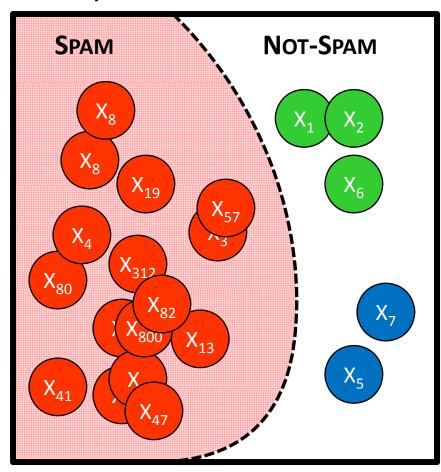
"One-Vs-All" Method

• Independently train binary classifier for each of the *C* classes



"One-Vs-All" Method

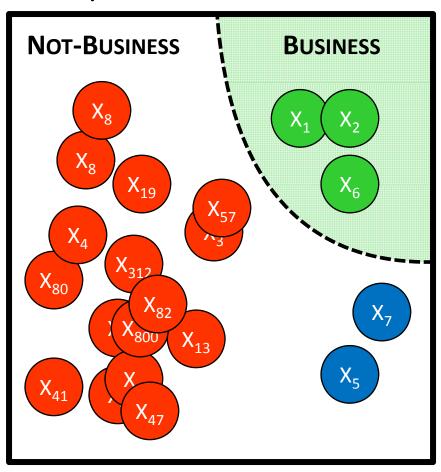
 Independently train binary classifier for each of the C classes Binary Classifier 1: **SPAM**



"One-Vs-All" Method

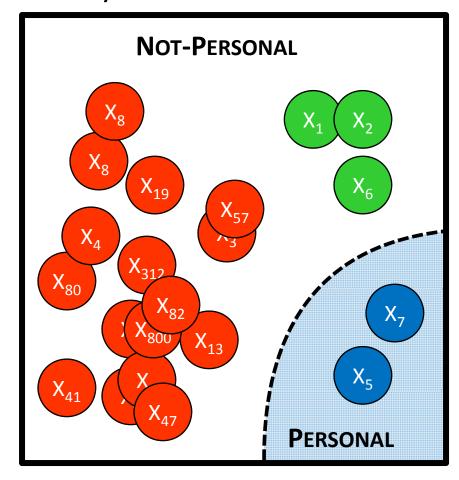
• Independently train binary classifier for each of the *C* classes

Binary Classifier 2: Business



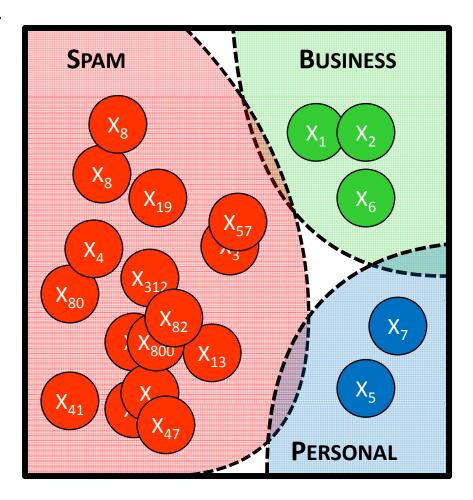
"One-Vs-All" Method

 Independently train binary classifier for each of the C classes Binary Classifier 3: **Personal**



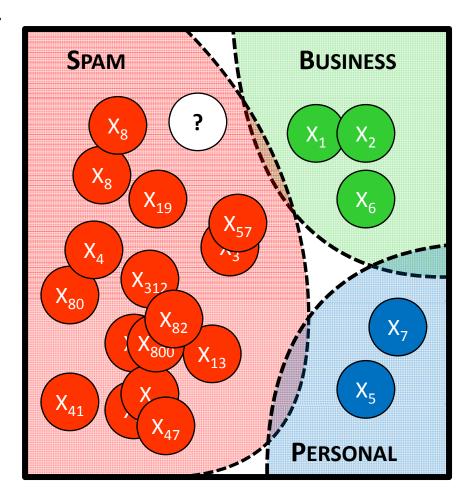
"One-Vs-All" Method

 Independently train binary classifier for each of the C classes



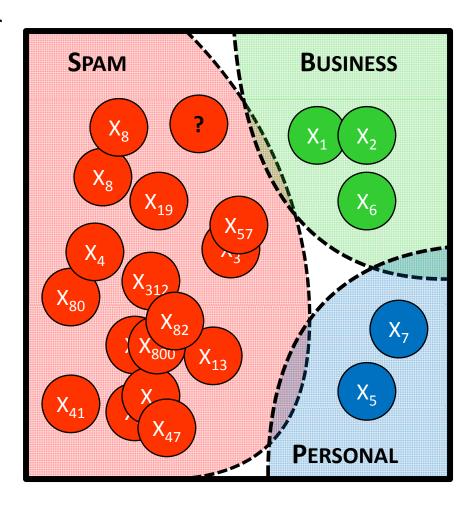
"One-Vs-All" Method

 Independently train binary classifier for each of the C classes



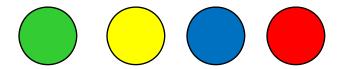
"One-Vs-All" Method

 Independently train binary classifier for each of the C classes

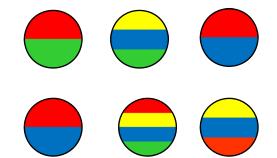


Multi-Label Data

Previous examples were single-label

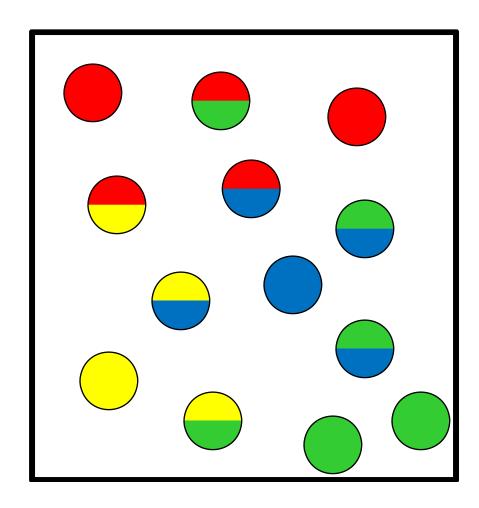


- However, real-world data is often *Multi-Label*
 - Each document can be assigned multiple labels
 - Labels not mutually exclusive

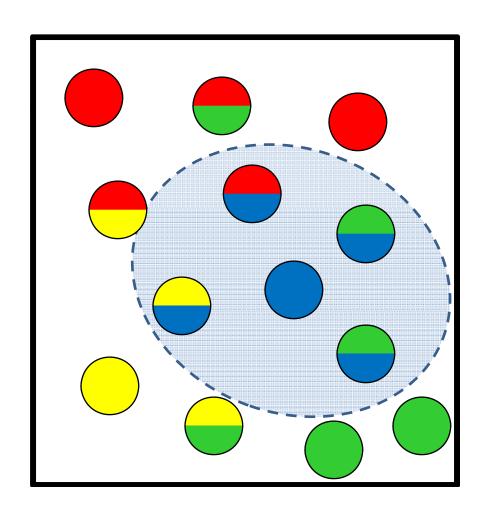


• E.g., A news story might be about **HEALTH** and **GENETICS** and **CANCER RESEARCH**

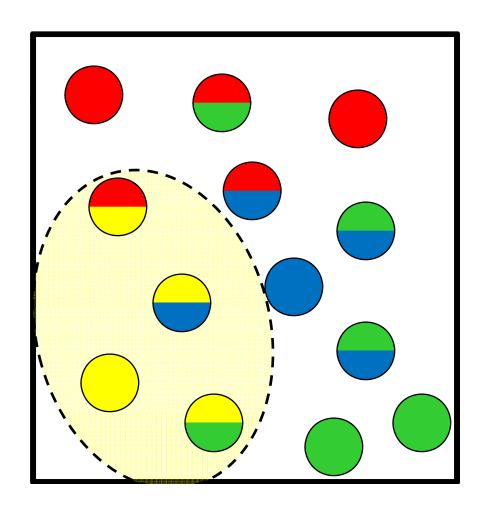
 Again, common solution is to use One-vs-All transformation



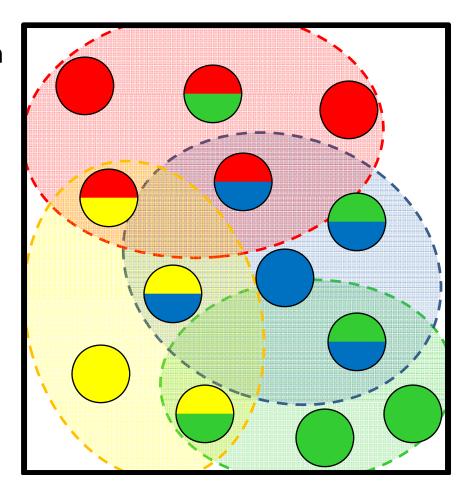
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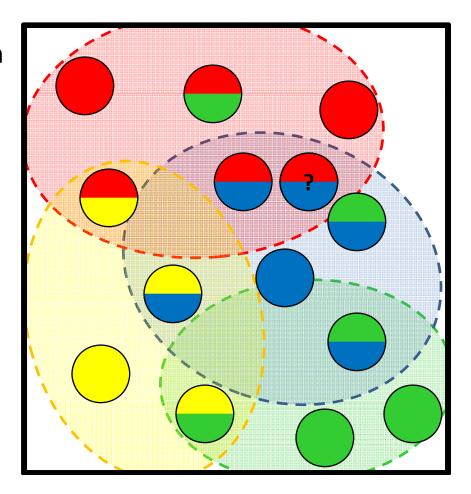
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- Again, common solution is to use One-vs-All transformation
- At test, must make a binary decision for each of the C classes



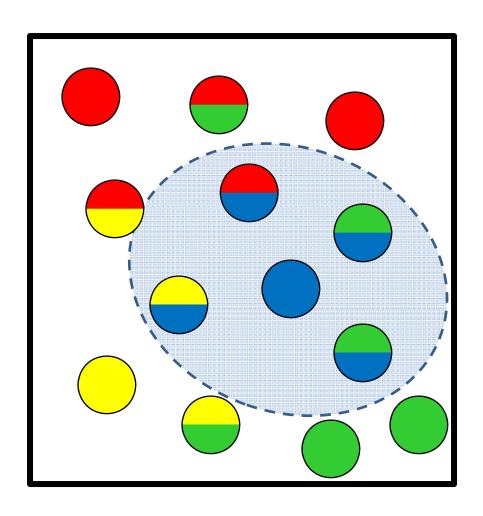
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- At test, must make a binary decision for each of the C classes



Binary SVMs: The Problem

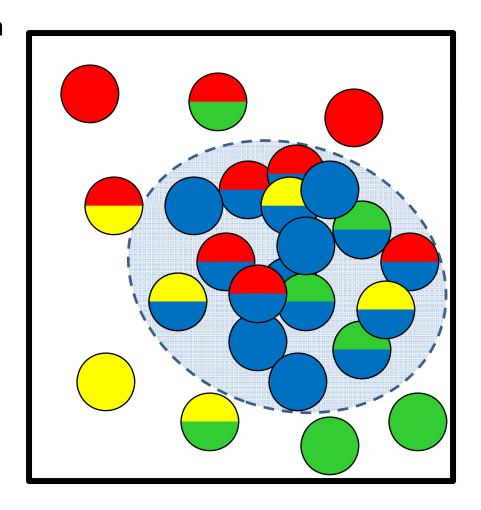
- All data is assumed to be relevant for each label
- Thus, green, red and yellow data is contaminating our model for blue
- Nonetheless, method often works well...

Why is this?



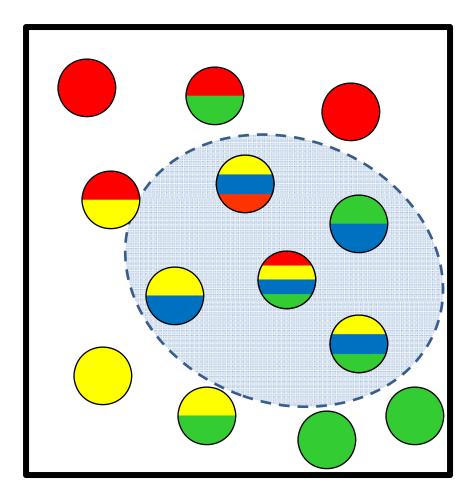
Binary SVMs: The Problem

- Depends on statistics of dataset
- Works fine with lots of training data



Binary SVMs: The Problem

- Depends on statistics of dataset
- Works fine with lots of training data
- However, becomes a problem as:
 - 1. The number of training documents becomes smaller
 - 2. The number of labels per document becomes larger



NY Times Article

Labels	Label Freq.
ANTITRUST ACTIONS AND LAWS	19
Suits and Litigation	67
VIDEO GAMES *	1

Article Excerpt

A flurry of lawsuits, started by a small American software developer, now surrounds the Nintendo Entertainment System...Atari Games argues that Nintendo's high degree of control is tantamount to monopoly, and is suing Nintendo for antitrust violations...

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Article Excerpt

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Models for VIDEO GAMES

SVM

nintendo

mcgowan

futuristic

compatible

illusion

shrewd

inception

truthful

profiles

billionayear

<u>suing</u>

infringement

architecture

handheld

tantamount

payoff

glut

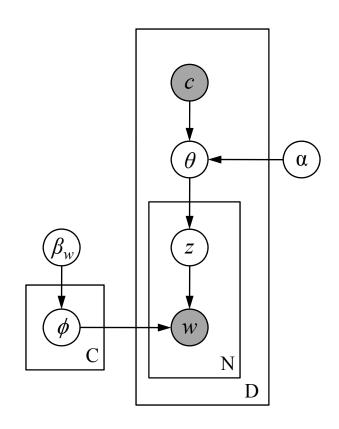
equitable

Models for VIDEO GAMES

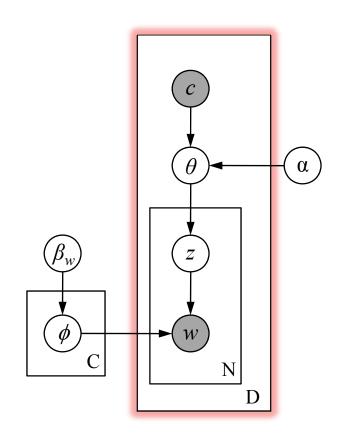
SVM	LDA
nintendo	nintendo
mcgowan	games
futuristic	software
compatible	video
illusion	system
shrewd	game
inception	chip
truthful	control
profiles	market
billionayear	home
<mark>suing</mark>	computer
<mark>infringement</mark>	shortage
architecture	say
handheld	buy
<u>tantamount</u>	demand
payoff	developer
glut	generally
equitable	japan

Overview

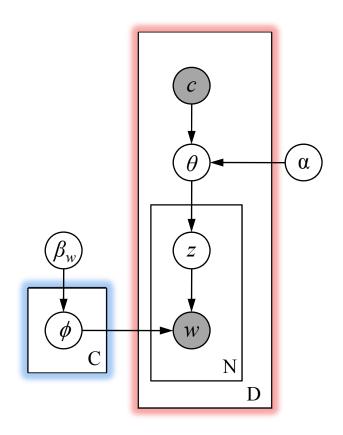
- Introduce the research problem
 - Research goals and challenges
- Motivate the use of probabilistic methods
- Present our probabilistic models
- Experimental Results



Documents

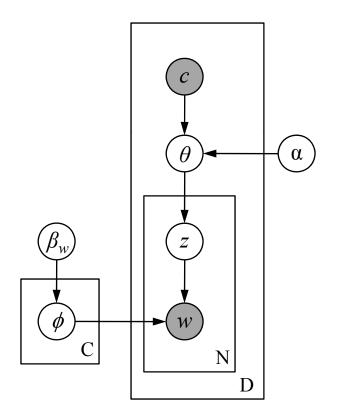


- Documents
- Labels



- Documents
- Labels

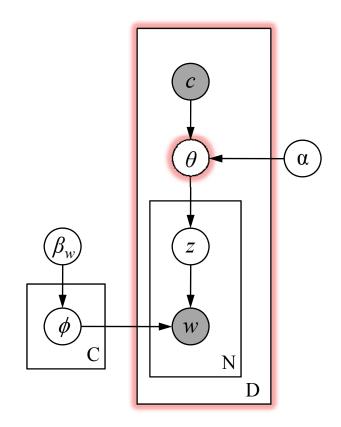
Mixture Model



- Documents
- Labels

Mixture Model

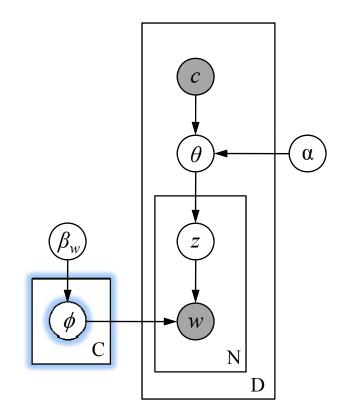
• Documents are mixtures of labels θ_d

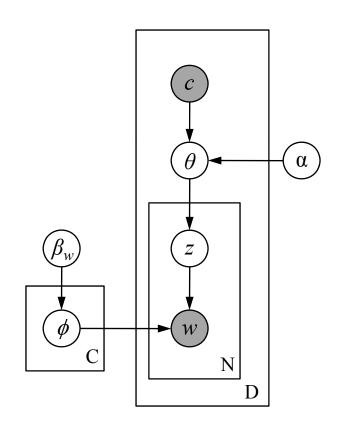


- Documents
- Labels

Mixture Model

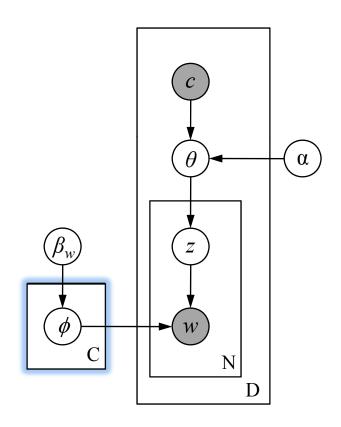
- Documents are mixtures of labels θ_d
- Labels are probability distributions over words ϕ_c



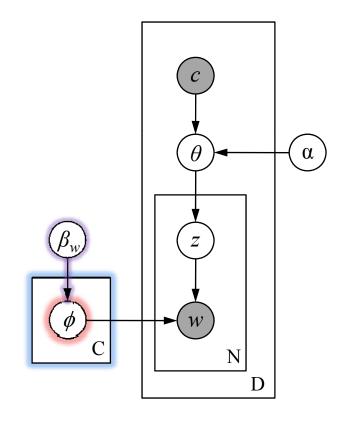


GENERATIVE PROCESS

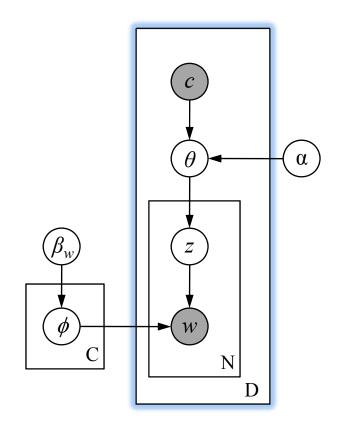
• For each label:



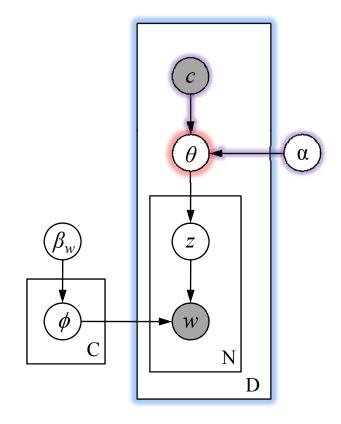
- For each label:
 - Sample a multinomial distribution over words ϕ_c from dirichlet β_w



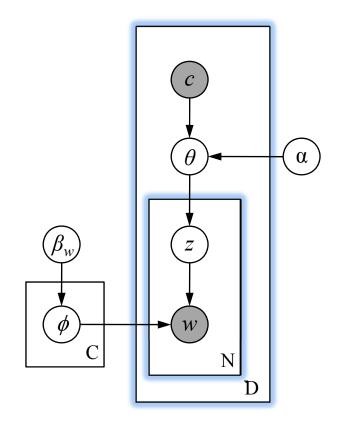
- For each label:
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- For each document:



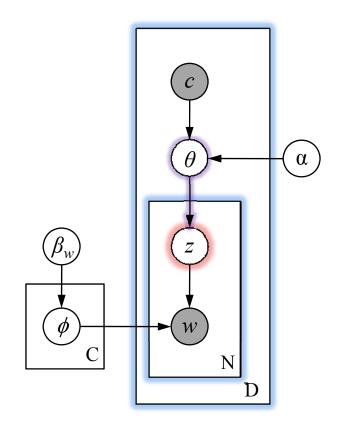
- For each label:
 - Sample a multinomial distribution over words ϕ_c from dirichlet β_w
- For each document:
 - Sample a multinomial distribution θ over the observed labels from dirichlet prior α'



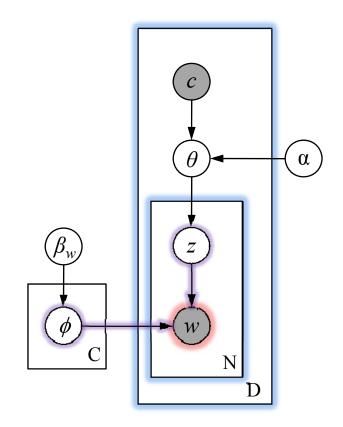
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- For each word in document:



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 - Sample a multinomial distribution over words ϕ_c from dirichlet β_w
- For each document:
 - Sample a multinomial distribution θ over the observed labels from dirichlet prior α'
- For each word in document:
 - Sample a label z

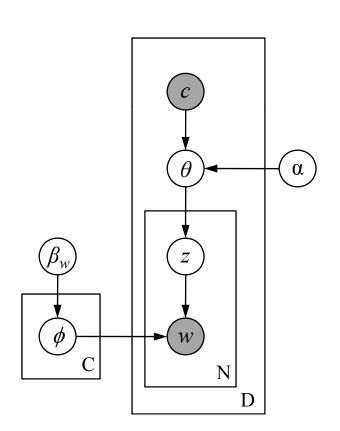


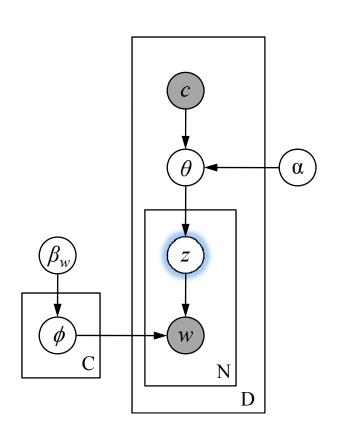
- For each label:
 - Sample a multinomial distribution over words ϕ_c from dirichlet β_w
- For each document:
 - Sample a multinomial distribution θ over the observed labels from dirichlet prior α'
- For each word in document:
 - Sample a label z
 - Generate a word w from ϕ_Z



• Training:

• Learn a distribution over words for each label, φ_c





Training:

- Learn a distribution over words for each label, φ_c
- Collapsed Gibbs sampler:
 - iteratively updating the z assignments of words to labels

LDA and rare labels

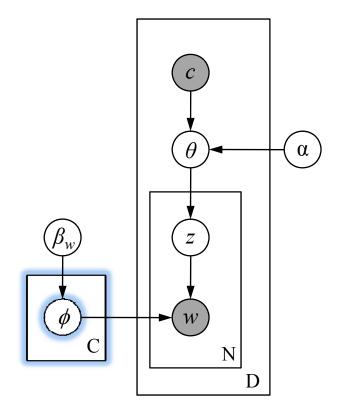
- Labels are learned simultaneously
- Words associated with well-known labels will be "explained away"

NY Times Article

Labels	Label Freq.
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Article Excerpt

A flurry of lawsuits, started by a small American software developer, now surrounds the Nintendo Entertainment System...Atari Games argues that Nintendo's high degree of control is tantamount to monopoly, and is suing Nintendo for antitrust violations...



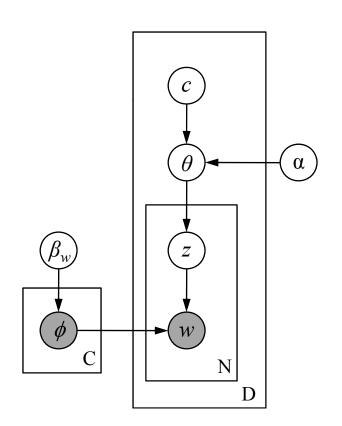
Label-Word Distributions

ARMS SALES ABROAD	176	ABORTION	24	ACID RAIN	11	AGNI MISSILE	1
iran	.021	abortion	.098	acid	.070	missile	.032
arms	.019	court	.033	rain	.067	india	.031
reagan	.014	abortions	.028	lakes	.028	technology	.016
house	.014	women	.017	environmental	.026	missiles	.016
president	.014	decision	.016	sulfur	.024	western	.015
north	.012	supreme	.016	study	.023	miles	.014
report	.011	rights	.015	emissions	.021	nuclear	.013
white	.011	judge	.015	plants	.021	indian	.013

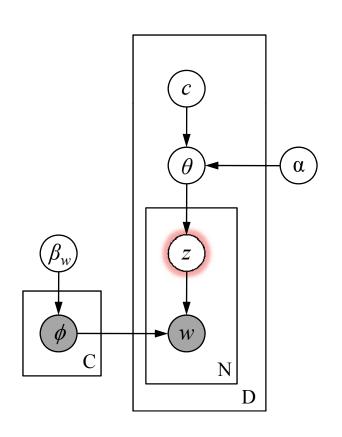
Inference for test-Documents

• Testing:

• Treat ϕ as observed



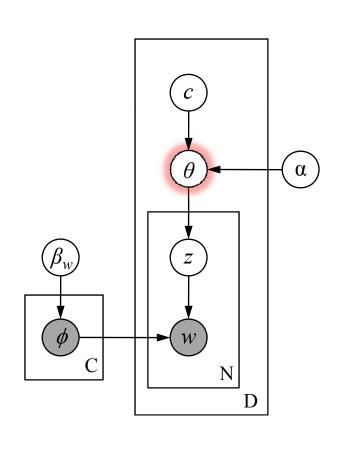
Inference for test-Documents



• Testing:

- Treat ϕ as observed
- Update z assignments for each test document to learn θ

Inference for test-Documents



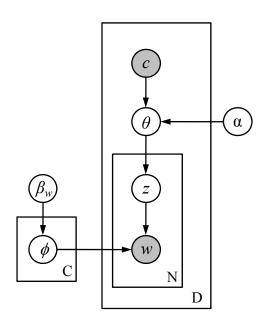
Testing:

- Treat ϕ as observed
- Update z assignments for each test document to learn θ

Predictions:

- Use θ as a predicted ranking of labels
- For binary predictions, threshold

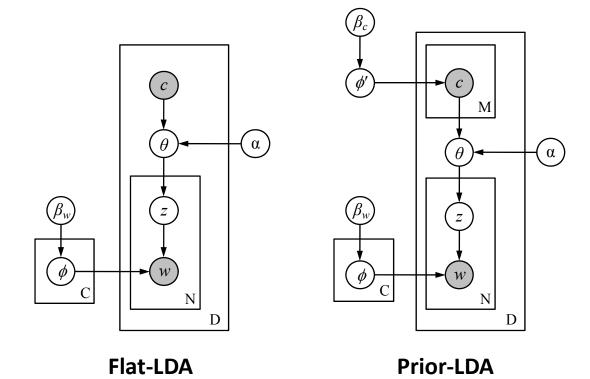
Model Extensions



Flat-LDA

Model Extensions

Account for baseline label frequencies



Prior-LDA

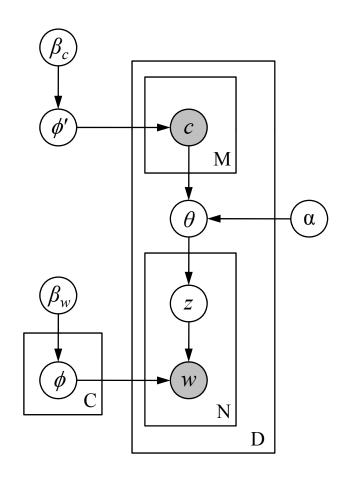
- Extends flat-LDA by incorporating a generative process for labels:
- Two-step generative process for each document

Generating Labels

• Sample labels, c, from a multinomial distribution ϕ' that reflects baseline label frequencies

Generating words

- Sample a document mixture over labels, θ , from a Dirichlet prior that is proportional to the number of times each label was sampled
 - α is now a vector of hyperparameters
- Given θ , generate each word as in Flat-LDA



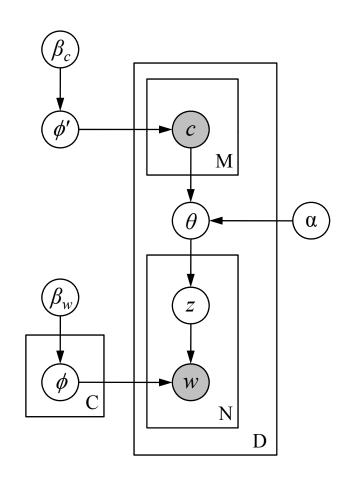
Prior-LDA

Training

- Learning ϕ is equivalent to Flat-LDA
 - Conditionally independent given *C*
- Estimate ϕ' directly from data

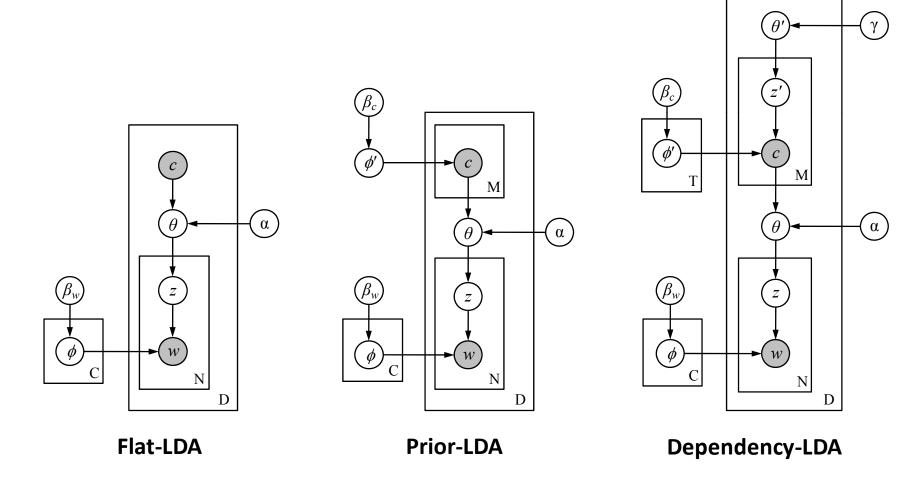
Test Time

- Same as Flat-LDA, except we now use an *informative* dirichlet prior on θ
- Vector of hyperparameters reflects baseline label freqs.



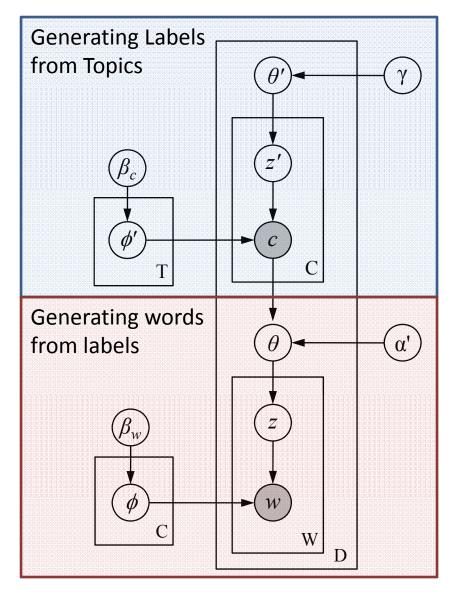
Model Extensions

Account for label dependencies



Dependency-LDA

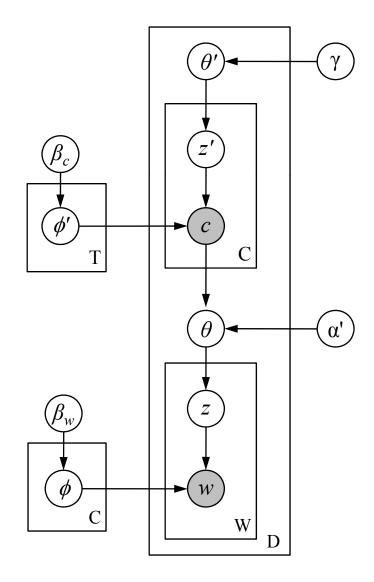
- Each document is a mixture of both
 - Topics θ'
 - Labels θ
- Topics are distributions over labels ϕ'
- Labels are distribution over words ϕ
- Three stage generative process for each document
 - 1. Generate labels from topics
 - 2. Sample θ conditioned on these labels
 - 3. Generate words as before



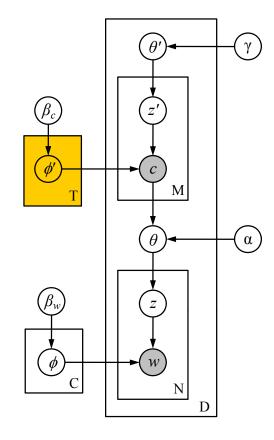
Inference

Training

- Independently train topic-word ϕ' and label-word ϕ distributions
 - Conditionally independent given c



Topic-Label Distributions

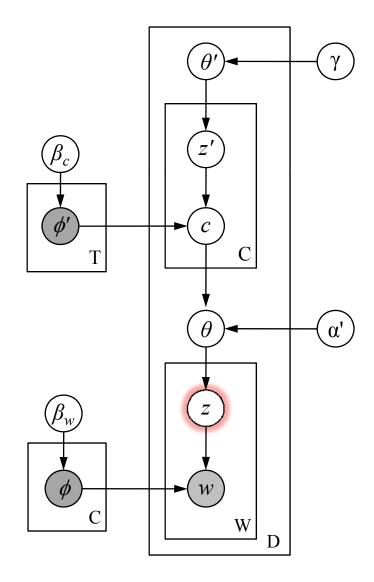


"Consumer Safety"	.017	"Warfare And Disputes"	.024
CANCER	.078	ARMAMENT, DEFENSE AND MILITARY	.162
HAZARDOUS AND TOXIC SUBSTANCES	.039	INTERNATIONAL RELATIONS	.133
PESTICIDES AND PESTS	.021	UNITED STATES INTERNATIONAL RELA	.132
RESEARCH	.021	CIVIL WAR AND GUERRILLA WARFARE	.098
SURGERY AND SURGEONS	.021	MILITARY ACTION	.053
TESTS AND TESTING	.021	CHEMICAL WARFARE	.029
FOOD	.018	REFUGEES AND EXPATRIATES	.019
RECALLS AND BANS OF PRODUCTS	.018	INDEPENDENCE MOVEMENTS	.013
CONSUMER PROTECTION	.016	BOUNDARIES AND TERRITORIAL ISSUES	.011
HEALTH, PERSONAL	.016	KURDS	.010

Inference

Test Time

• Fix ϕ and ϕ' distributions



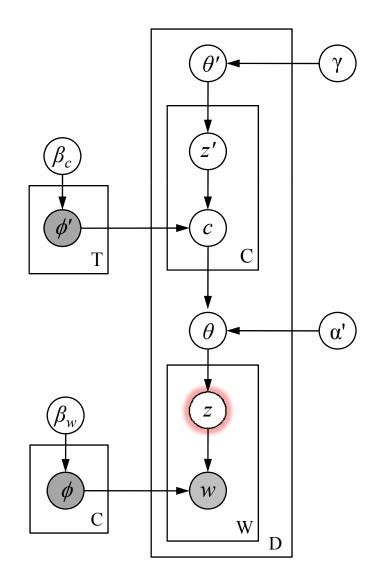
Inference

Test Time

• Fix ϕ and ϕ' distributions

Update Sequence

1. Update all z assignments

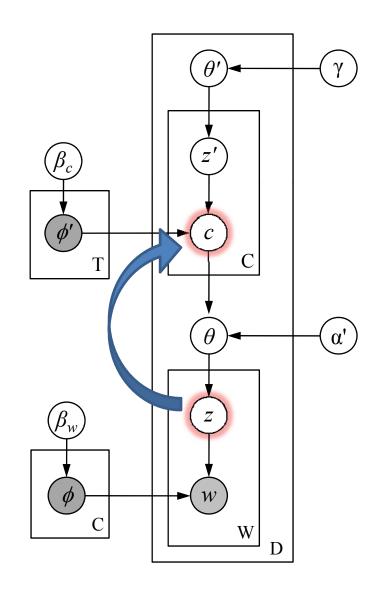


Test Time

• Fix ϕ and ϕ' distributions

Update Sequence

- 1. Update all z assignments
- 2. Set c equal to z

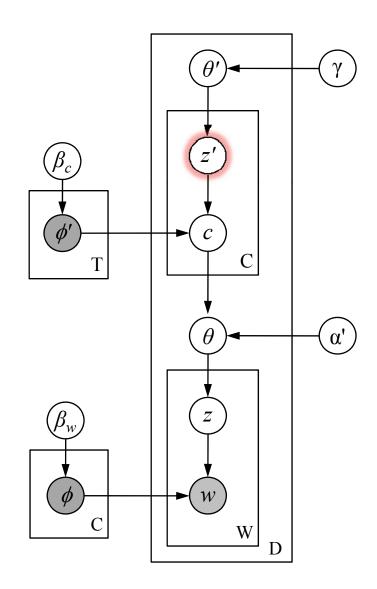


Test Time

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- 2. Set c equal to z
- 3. Update all z' assignments



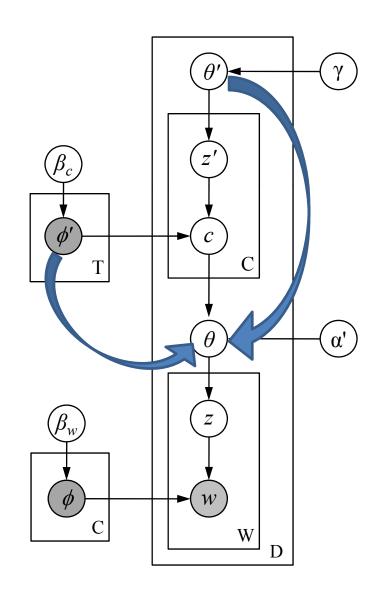
Test Time

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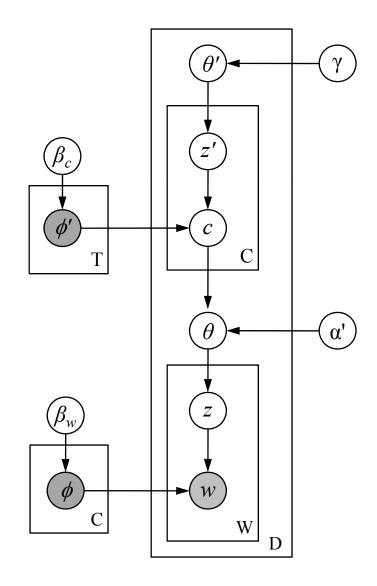
Update Sequence

- 1. Update all z assignments
- 2. Set c equal to z
- 3. Update all z' assignments
- 4. Compute hyperparameter vector α' :

$$\alpha'^{(d)} = \eta \cdot \phi'^{(\cdot)} \cdot \theta'^{(d)}$$



- Key here is that we learn a document-specific prior on θ
 - Reflects label dependencies



Example – Predictions

New York Times Article

LEAD: The special Senate and House committees investigating the Irancontra affair decided today to hold joint hearings, and set a timetable for granting limited immunity from prosecution to the two central witnesses. The extraordinary agreement, which also calls for merging the committee staffs and for sharing evidence, is expected to speed the inquiry...

True Document Labels	Label Freq
IMMUNITY FROM PROSECUTION	4
ARMS SALES ABROAD	176
ARMAMENT, DEFENSE AND MILITARY FORCES	409
UNITED STATES INTERNATIONAL RELATIONS	630

Example – Predictions

New York Times Article

LEAD: The special Senate and House committees investigating the Irancontra affair decided today to hold joint hearings, and set a timetable for granting limited immunity from prosecution to the two central witnesses. The extraordinary agreement, which also calls for merging the committee staffs and for sharing evidence, is expected to speed the inquiry...

True Document Labels	Label Freq
IMMUNITY FROM PROSECUTION	4
ARMS SALES ABROAD	176
ARMAMENT, DEFENSE AND MILITARY FORCES	409
LINITED STATES INTERNATIONAL RELATIONS	630

Binary SVMs

- 1 CONGRESSIONAL INVESTIGATIONS
- 2 ARMS SALES ABROAD
- 3 ARMAMENT, DEFENSE AND MILITARY FORCES
- 4 UNITED STATES INTERNATIONAL RELATIONS
- CIVIL WAR AND GUERRILLA WARFARE
- 6 ETHICS
- 7 DISCLOSURE OF INFORMATION
- 8 FOREIGN AID
- 9 UNITED STATES ARMAMENT AND DEFENSE
- 10 LAW AND LEGISLATION

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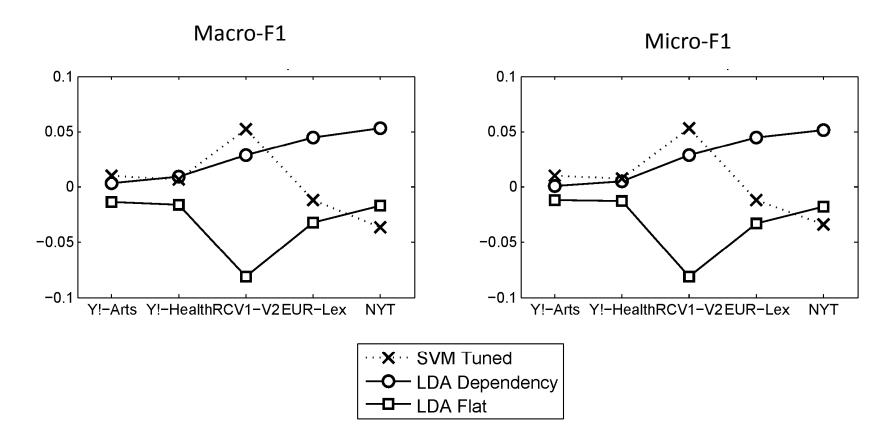
	Binary SVMs	LDA - Flat	р	LDA - Prior	р	LDA - Dependencies	р
1	CONGRESSIONAL INVESTIGATIONS	ARMS SALES ABROAD	.204	ARMS SALES ABROAD	.261	ARMS SALES ABROAD	.291
2	ARMS SALES ABROAD	CONGRESSIONAL INVESTIGATIONS	.182	CONGRESSIONAL INVESTIGATIONS	.237	CONGRESSIONAL INVESTIGATIONS	.234
3	ARMAMENT, DEFENSE AND MILITARY FORCES	LAW AND LEGISLATION	.059	LAW AND LEGISLATION	.102	UNITED STATES INTERNATIONAL RELATIONS	.110
4	UNITED STATES INTERNATIONAL RELATIONS	IMMUNITY FROM PROSECUTION	.042	IMMUNITY FROM PROSECUTION	.062	LAW AND LEGISLATION	.100
5	CIVIL WAR AND GUERRILLA WARFARE	ETHICS	.004	ETHICS	.045	IMMUNITY FROM PROSECUTION	.063
6	ETHICS	MIDGETMAN (MISSILE)	.003	UNITED STATES INTERNATIONAL RELATIONS	.024	ARMAMENT, DEFENSE AND MILITARY FORCES	.049
7	DISCLOSURE OF INFORMATION	VETOES (US)	.003	TRIALS	.018	CIVIL WAR AND GUERRILLA WARFARE	.014
8	FOREIGN AID	UNITED STATES ARMAMENT AND DEFENSE	.003	UNITED STATES ARMAMENT AND DEFENSE	.010	DECISIONS AND VERDICTS	.007
9	UNITED STATES ARMAMENT AND DEFENSE	CONGRESSIONAL COMMITTEES	.003	INTERNATIONAL RELATIONS	.008	FOREIGN AID	.007
10	LAW AND LEGISLATION	B-2 AIRPLANE	.003	FINANCES	.007	TRIALS	.005

Overview

- Introduce the research problem
 - Research goals and challenges
- Motivate the use of probabilistic methods
- Present our probabilistic models
- Experimental Results

Full set of experiments

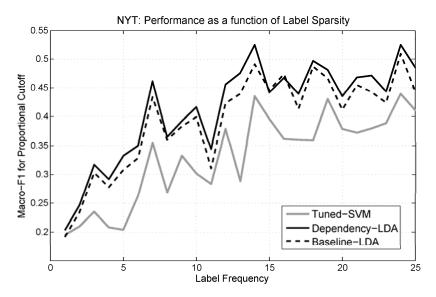
- 5 datasets
- 5 models
 - 2 SVM methods
 - 3 LDA-based models
- 2 prediction tasks
 - 13 evaluation metrics



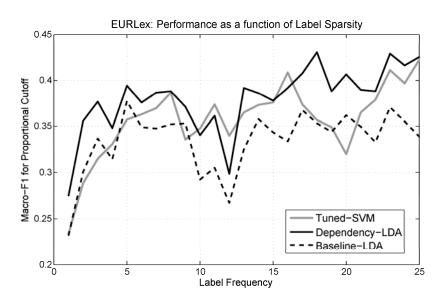
Dataset results, sorting in terms of *increasing* #labels/document

F1 Performance on Rare Labels

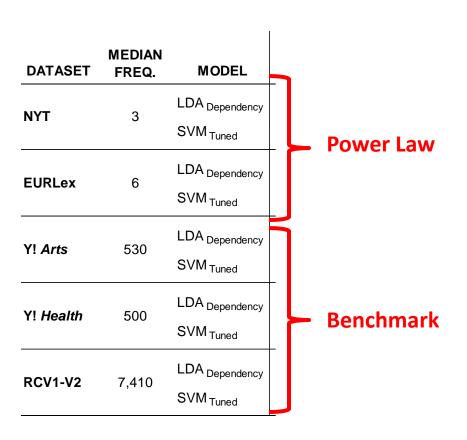




EUR-Lex



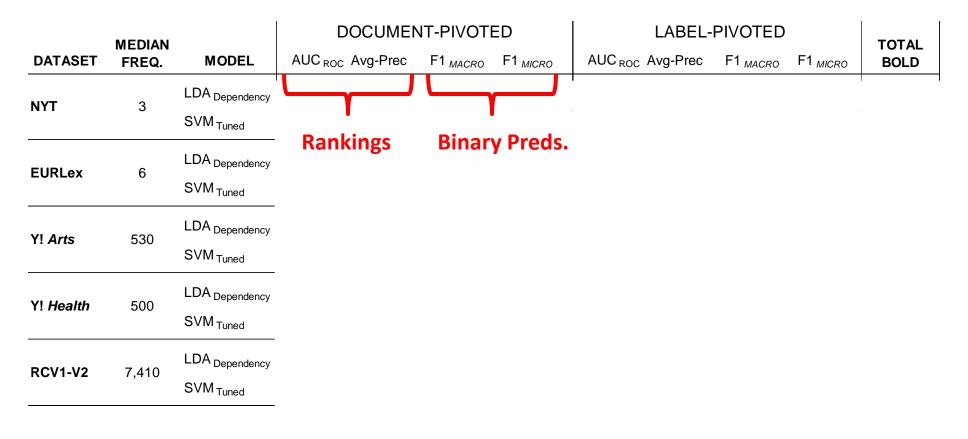
DATASET	MEDIAN FREQ.	MODEL	
NYT	3	LDA _{Dependency} SVM _{Tuned}	
EURLex	6	LDA _{Dependency} SVM _{Tuned}	
Y! Arts	530	LDA _{Dependency} SVM _{Tuned}	
Y! Health	500	LDA _{Dependency} SVM _{Tuned}	
RCV1-V2	7,410	LDA _{Dependency}	



Evaluation Metrics

	MEDIAN		DOCUMEN	NT-PIVOTI	ED	LABEL-PIVOTED				
DATASET	FREQ.	MODEL	AUC ROC Avg-Prec	F1 _{MACRO}	F1 _{MICRO}	AUC ROC Avg-Prec	F1 _{MACRO}	F1 _{MICRO}	TO B(
NYT	3	LDA _{Dependency}	l							
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Y! Arts	530	LDA _{Dependency}								
Y! Health	500	LDA _{Dependency}								
RCV1-V2	7,410	LDA _{Dependency}								

Evaluation Metrics



Evaluation Metrics

	MEDIAN		D	OCUMEN	NT-PIVOTI	ΕD		TOTAL			
DATASET	FREQ.	MODEL	AUC ROC	Avg-Prec	F1 _{MACRO}	F1 _{MICRO}	AUC _{ROC}	Avg-Prec	F1 _{MACRO}	F1 _{MICRO}	BOLD
NYT	3	LDA _{Dependency}	.991	.631	.542	.539	.958	.383	.325	.541	8
NT I	3	SVM _{Tuned}	.965	.492	.453	.453	.959	.309	.270	.487	1
EURLex	6	LDA _{Dependency}	.982	.511	.458	.461	.958	.472	.382	.467	8
EURLEX	O	SVM _{Tuned}	.967	.430	.402	.405	.960	.466	.373	.471	2
Y! Arts	530	LDA _{Dependency}	.855	.630	.454	.416	.755	.341	.367	.451	6
1: Arts		SVM _{Tuned}	.833	.625	.461	.425	.757	.330	.355	.454	4
Y! Health	500	LDA _{Dependency}	.926	.805	.619	.577	.850	.569	.562	.646	6
1: Health	300	SVM _{Tuned}	.898	.788	.617	.580	.849	.570	.571	.656	6
RCV1-V2	7,410	LDA _{Dependency}	.987	.873	.743	.733	.971	.559	.539	.762	1
RCV1-V2	7,410	SVM _{Tuned}	.988	.896	.767	.757	.981	.608	.579	.787	8

SCALE OF DIFFERENCES

	DO	OCUMEN	NT-PIVOT	ED		LABEL-			
DATASET	AUC ROC	Avg-Prec	F1 _{MACRO}	F1 _{MICRO}	AUC _{ROC}	Avg-Prec	F1 _{MACRO}	F1 _{MICRO}	AVG.
NYT	.026	.139	.090	.085	001	.074	.055	.054	.065
EURLex	.015	.081	.057	.056	002	.006	.009	004	.027
Y! Arts	.022	.005	007	009	002	.010	.012	004	.003
Y! Health	.027	.017	.002	003	.001	001	009	010	.003
RCV1-V2	001	023	024	024	010	049	041	025	025

GREEN: LDA > SVM

RED: SVM>LDA

SCALE OF DIFFERENCES

	DO	OCUMEI	NT-PIVOT	ED		LABEL-				
DATASET	AUC _{ROC}	Avg-Prec	F1 _{MACRO}	F1 _{MICRO}	AUC ROC	Avg-Prec	F1 _{MACRO}	F1 _{MICRO}	AVG.	
NYT	.026	.139	.090	.085	001	.074	.055	.054	.065	•
EURLex	.015	.081	.057	.056	002	.006	.009	004	.027	
Y! Arts	.022	.005	007	009	002	.010	.012	004	.003	
Y! Health	.027	.017	.002	003	.001	001	009	010	.003	
RCV1-V2	001	023	024	024	010	049	041	025	025	
	l				I					
										•

GREEN: LDA > SVM

RED: SVM>LDA

Comparison with Published Values

Comparison with Published Values

		Avg-Prec	Rnk-Loss	One-Err	Is-Err	Margin
	MLNB	1.1	22.9	100.0	99.6	1644.0
1 epoch	BR	26.9	40.4	48.7	98.6	3230.7
2 epochs	BR	31.6	35.5	41.5	98.2	3050.1
5 epochs	BR	35.9	31.0	37.3	97.2	2842.6
1 epoch	MMP	29.3	3.9	75.9	98.8	597.6
2 epochs		39.5	4.4	54.4	97.5	694.1
5 epochs	MMP	47.3	4.7	40.2	96.0	761.2
1 epoch	DMLPP	46.7	2.8	35.5	97.9	433.9
2 epochs	DMLPP	52.3	2.5	29.5	96.6	397.1
	LDA Dependency	51.1	1.8	32.0	97.2	269.2

Mencia, Furnkranz (2010)

Future Work

- Hybrid Discriminative / Generative extensions to the model
- Alternative methods for combining strength of both discriminative and generative approaches
- Any suggestions...?

Special Thanks

- America Holloway
- Padhraic Smyth
- Mark Steyvers
- All MADLabbers